

Inference in Nonlinear Dynamical Systems with Dynamic Stream Weights for Audiovisual Speaker Tracking

ICA 2019

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RUHR
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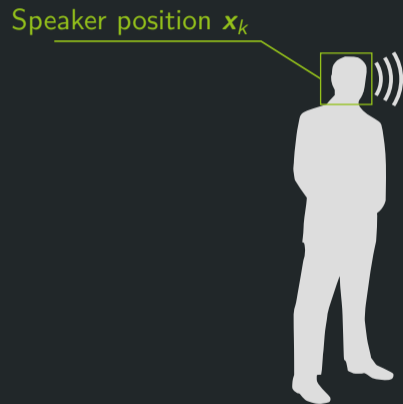
Audiovisual speaker tracking



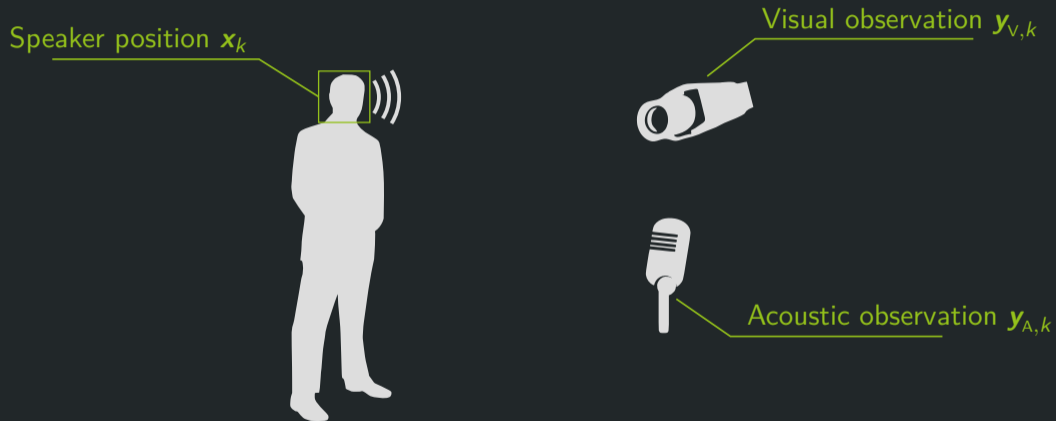
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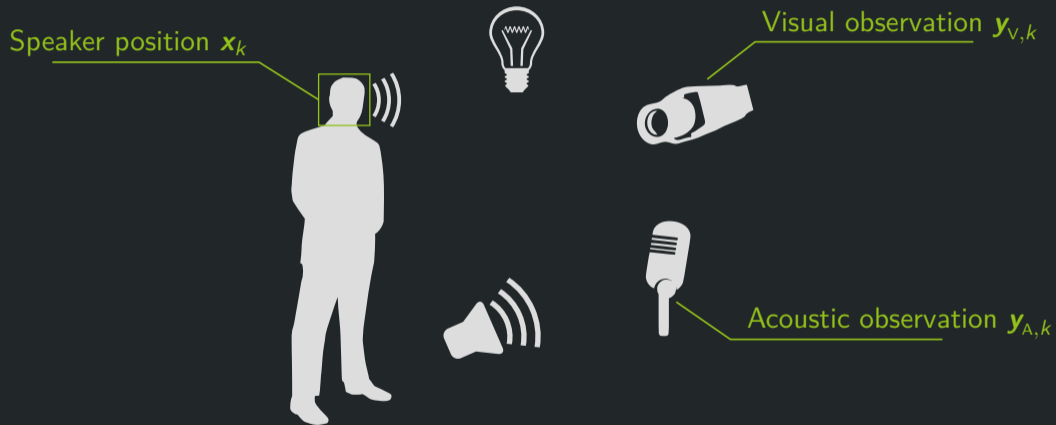
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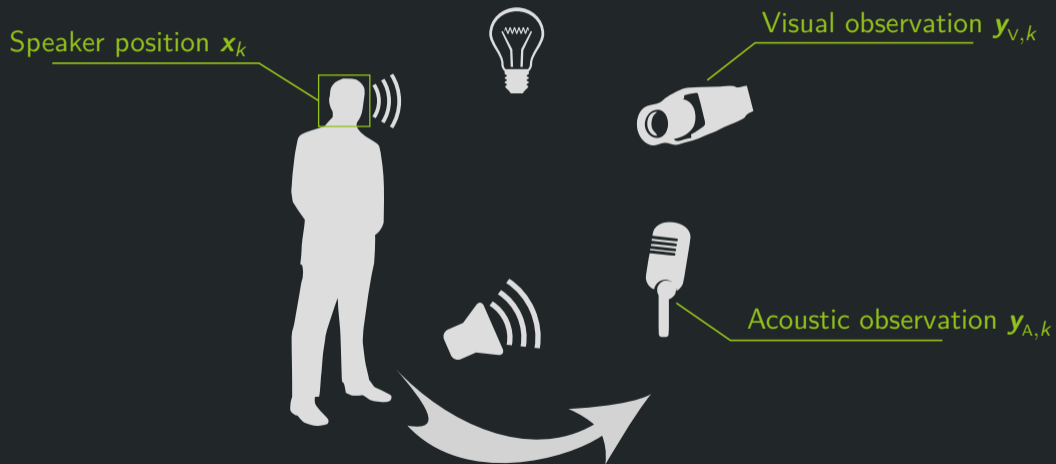
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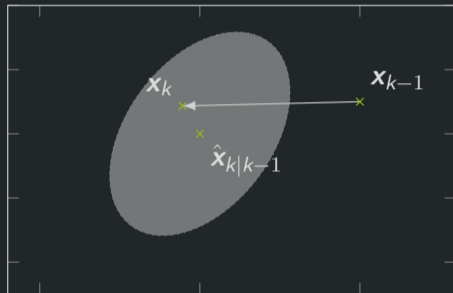


Audiovisual speaker tracking

Prediction step

System dynamics:

$$\mathbf{x}_k = f(\mathbf{x}_{k-1}) + \mathbf{v}_k, \quad \mathbf{v}_k = \mathcal{N}(\mathbf{0}, \mathbf{Q})$$

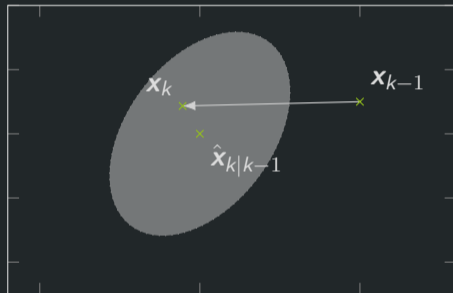


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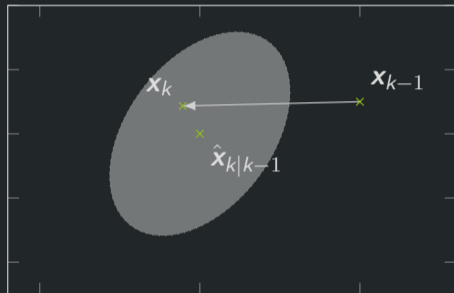
$$p(\mathbf{x}_k | \mathbf{Y}_{A,k-1}, \mathbf{Y}_{V,k-1}) = \int p(\mathbf{x}_k | \mathbf{x}_{k-1}) p(\mathbf{x}_{k-1} | \mathbf{Y}_{A,k-1}, \mathbf{Y}_{V,k-1}) d\mathbf{x}_{k-1}$$

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$$p(\mathbf{x}_k | \mathbf{Y}_{A,k-1}, \mathbf{Y}_{V,k-1}) = \int \underbrace{p(\mathbf{x}_k | \mathbf{x}_{k-1})}_{\text{Dynamic model}} \underbrace{p(\mathbf{x}_{k-1} | \mathbf{Y}_{A,k-1}, \mathbf{Y}_{V,k-1})}_{\text{Prior}} d\mathbf{x}_{k-1}$$

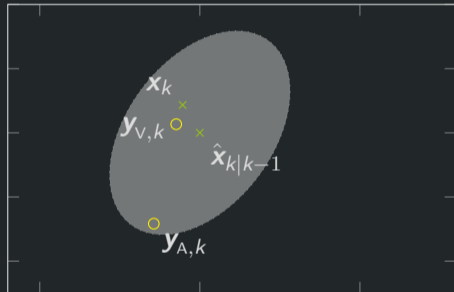
Audiovisual speaker tracking

Observation

Observation model:

$$\mathbf{y}_k = \begin{bmatrix} \mathbf{y}_{A,k} & \mathbf{y}_{V,k} \end{bmatrix}^T = h(\mathbf{x}_k) + \mathbf{w}_k$$

$$\mathbf{w}_k = \mathcal{N}(\mathbf{0}, \mathbf{R}), \quad \mathbf{R} = \begin{bmatrix} \mathbf{R}_{AA} & \mathbf{R}_{AV} \\ \mathbf{R}_{VA} & \mathbf{R}_{VV} \end{bmatrix}$$



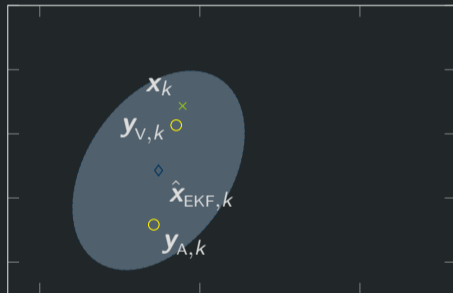
Audiovisual speaker tracking

Update step (standard Kalman filter)

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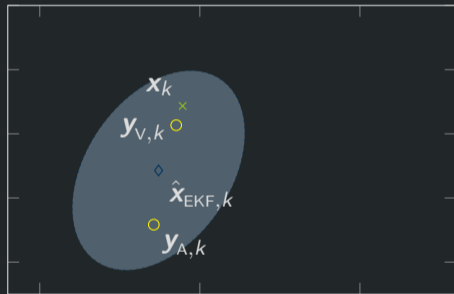
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$$p(\mathbf{x}_k | \mathbf{Y}_{A,k}, \mathbf{Y}_{V,k}) \propto p(\mathbf{x}_k | \mathbf{Y}_{A,k-1}, \mathbf{Y}_{V,k-1}) p(\mathbf{y}_{A,k}, \mathbf{y}_{V,k} | \mathbf{x}_k)$$

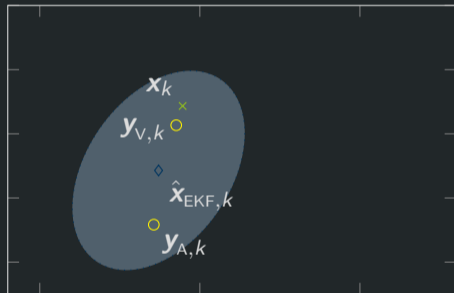
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$$p(\mathbf{x}_k | \mathbf{Y}_{A,k}, \mathbf{Y}_{V,k}) \propto p(\mathbf{x}_k | \mathbf{Y}_{A,k-1}, \mathbf{Y}_{V,k-1}) \underbrace{p(\mathbf{y}_{A,k}, \mathbf{y}_{V,k} | \mathbf{x}_k)}_{\text{Sensor model}}$$

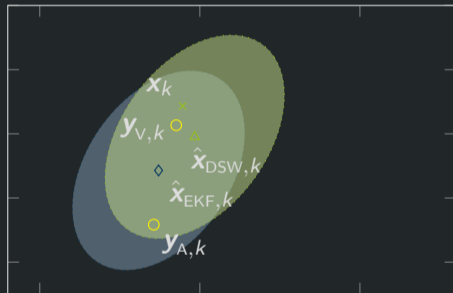
Audiovisual speaker tracking

Update step (Kalman filter with dynamic stream weights¹)

Observation model:

$$\mathbf{y}_{A,k} = h_A(\mathbf{x}_k) + \mathbf{w}_{A,k}, \quad \mathbf{w}_{A,k} = \mathcal{N}(\mathbf{0}, \mathbf{R}_{AA})$$

$$\mathbf{y}_{V,k} = h_V(\mathbf{x}_k) + \mathbf{w}_{V,k}, \quad \mathbf{w}_{V,k} = \mathcal{N}(\mathbf{0}, \mathbf{R}_{VV})$$



¹C. Schymura et al.: *Extending linear dynamical systems with dynamic stream weights for audiovisual speaker localization*, IWAENC, 2018

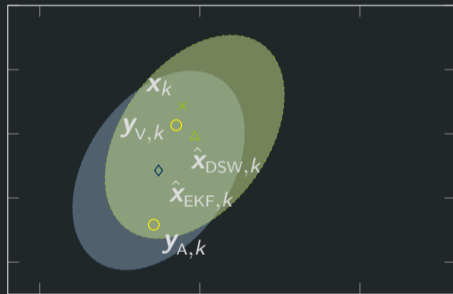
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¹C. Schymura et al.: *Extending linear dynamical systems with dynamic stream weights for audiovisual speaker localization*, IWAENC, 2018

Inference

Extended Kalman filter approach: first-order Taylor series expansion

$$f(\mathbf{x}_{k-1}) \approx f(\hat{\mathbf{x}}_{k-1}) + \mathbf{F}(\hat{\mathbf{x}}_{k-1})(\mathbf{x}_{k-1} - \hat{\mathbf{x}}_{k-1})$$

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$$\Rightarrow p(\mathbf{x}_k | \mathbf{Y}_{A,k-1}, \mathbf{Y}_{V,k-1}) = \mathcal{N}\left(\mathbf{x}_k | \hat{\mathbf{x}}_{k-1}, \hat{\Sigma}_{k-1}\right)$$

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Prediction step (identical to standard EKF)

$$\hat{\mathbf{x}}_{k|k-1} = f(\hat{\mathbf{x}}_{k-1})$$

$$\hat{\Sigma}_{k|k-1} = \mathbf{F}_{k-1} \hat{\Sigma}_{k-1} \mathbf{F}_{k-1}^T + \mathbf{Q}, \quad \mathbf{F}_{k-1} \equiv \mathbf{F}(\hat{\mathbf{x}}_{k-1}) = \left. \frac{\partial f(\mathbf{x}_{k-1})}{\partial \mathbf{x}_{k-1}} \right|_{\mathbf{x}_{k-1} = \hat{\mathbf{x}}_{k-1}}$$

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Extended Kalman filter approach: first-order Taylor series expansion

$$h_{\{A,V\}}(\mathbf{x}_k) \approx h_{\{A,V\}}(\hat{\mathbf{x}}_k) + \mathbf{H}_{\{A,V\},k}(\mathbf{x}_k - \hat{\mathbf{x}}_k), \quad \mathbf{H}_{\{A,V\},k} \equiv \left. \frac{\partial h_{\{A,V\}}(\mathbf{x}_k)}{\partial \mathbf{x}_k} \right|_{\mathbf{x}_k = \hat{\mathbf{x}}_k}$$

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Update step

$$\begin{bmatrix} \mathbf{K}_{A,k}^T \\ \mathbf{K}_{V,k}^T \end{bmatrix} = \begin{bmatrix} \mathbf{R}_A + \lambda_k \mathbf{H}_{A,k} \hat{\Sigma}_{k|k-1} \mathbf{H}_{A,k}^T & (1 - \lambda_k) \mathbf{H}_{A,k} \hat{\Sigma}_{k|k-1} \mathbf{H}_{V,k}^T \\ \lambda_k \mathbf{H}_{V,k} \hat{\Sigma}_{k|k-1} \mathbf{H}_{A,k}^T & \mathbf{R}_V + (1 - \lambda_k) \mathbf{H}_{V,k} \hat{\Sigma}_{k|k-1} \mathbf{H}_{V,k}^T \end{bmatrix}^{-1} \begin{bmatrix} \mathbf{H}_{A,k} \\ \mathbf{H}_{V,k} \end{bmatrix} \hat{\Sigma}_{k|k-1} \quad (1)$$

$$\hat{\mathbf{x}}_k = \hat{\mathbf{x}}_{k|k-1} + \lambda_k \mathbf{K}_{A,k} (\mathbf{y}_{A,k} - h_A(\hat{\mathbf{x}}_k)) + (1 - \lambda_k) \mathbf{K}_{V,k} (\mathbf{y}_{V,k} - h_V(\hat{\mathbf{x}}_k))$$

$$\hat{\Sigma}_{k|k-1} = \left(\mathbf{I} - \lambda_k \mathbf{K}_{A,k} \mathbf{H}_{A,k} - (1 - \lambda_k) \mathbf{K}_{V,k} \mathbf{H}_{V,k} \right) \hat{\Sigma}_{k|k-1}$$

Inference

The system of linear matrix equations in Eq. (1) can be expressed as

$$\begin{bmatrix} \mathbf{K}_{A,k}^T & \mathbf{K}_{V,k}^T \end{bmatrix}^T = \left[\mathbf{R} + \mathbf{U}_k \mathbf{W}_k \mathbf{U}_k^T \right]^{-1} \begin{bmatrix} \mathbf{H}_{A,k} & \mathbf{H}_{V,k} \end{bmatrix}^T \hat{\Sigma}_{k|k-1}$$

$$\mathbf{R} = \text{blkdiag}(\mathbf{R}_A, \mathbf{R}_V), \quad \mathbf{U}_k = \text{blkdiag}(\mathbf{H}_{A,k}, \mathbf{H}_{V,k}), \quad \mathbf{W}_k = \begin{bmatrix} \lambda_k & 1 - \lambda_k \\ \lambda_k & 1 - \lambda_k \end{bmatrix} \otimes \hat{\Sigma}_{k|k-1}$$

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Modified Kalman gain computation using the binomial inverse theorem²

$$\begin{bmatrix} \mathbf{K}_{A,k}^T & \mathbf{K}_{V,k}^T \end{bmatrix}^T = \left[\mathbf{R}^{-1} - \mathbf{R}^{-1} \mathbf{U}_k \mathbf{\Gamma}_k \mathbf{U}_k^T \mathbf{R}^{-1} \right] \begin{bmatrix} \mathbf{H}_{A,k} & \mathbf{H}_{V,k} \end{bmatrix}^T \hat{\Sigma}_{k|k-1}, \quad \mathbf{\Gamma}_k = \mathbf{W}_k \left(\mathbf{I} + \mathbf{U}_k^T \mathbf{R}^{-1} \mathbf{U}_k \mathbf{W}_k \right)^{-1}$$

²D. Harville: *Extension of the Gauss-Markov theorem to include the estimation of random effects*, Ann. Statist. vol.4, no. 2, 1976

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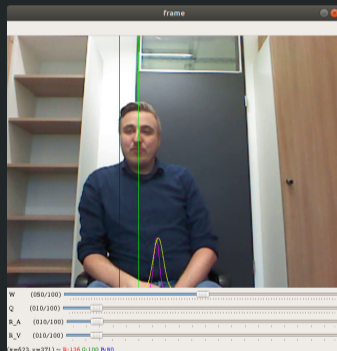
Complexity w.r.t. matrix inversions: $\mathcal{O}\left(8D_x^3\right)$ vs. $\mathcal{O}\left((D_{y_A} + D_{y_V})^3\right)$

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Evaluation

Experimental setup

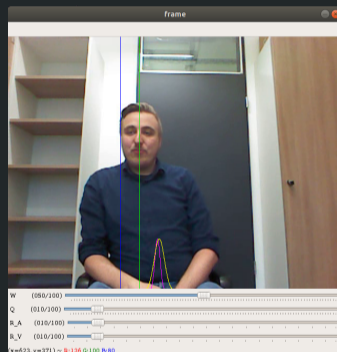
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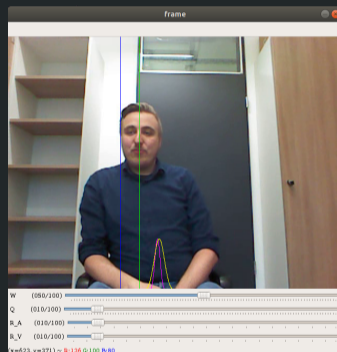


³C. Schymura et al.: *Audiovisual speaker tracking using nonlinear dynamical systems with dynamic stream weights*, arXiv, 2019

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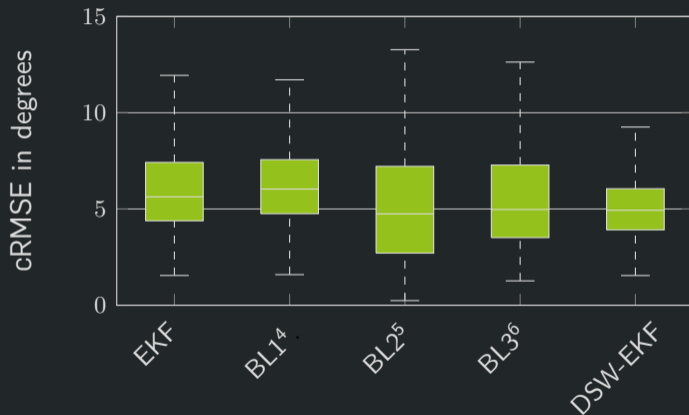
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- ▶ Four baseline systems: standard EKF, one KF-based and two particle filter-based systems.
- ▶ Leave-one-out cross-validation paradigm.



³C. Schymura et al.: *Audiovisual speaker tracking using nonlinear dynamical systems with dynamic stream weights*, arXiv, 2019

Evaluation

Results



⁴T. Gehrig et al.: *Kalman filters for audio-video source localization*, WASPAA, 2005

⁵S. Gerlach et al.: *2D audio-visual localization in home environments using a particle filter*, ITG Symp., 2012

⁶X. Qian et al.: *3D audio-visual speaker tracking with an adaptive particle filter*, ICASSP, 2017

Conclusions and outlook

- ▶ DSW-based audiovisual speaker tracking frameworks can be extended to cope with nonlinear systems.

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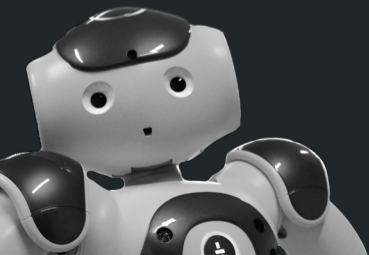
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Thank you for your attention!