# A Dynamic Stream Weight Backprop Kalman Filter for Audiovisual Speaker Tracking

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Observation functions:

$$oldsymbol{y}_{ extsf{A},k} = oldsymbol{\mathcal{C}}_{ extsf{A}}oldsymbol{x}_k$$

$$oldsymbol{y}_{{\scriptscriptstyle ee},k}=oldsymbol{\mathcal{C}}_{{\scriptscriptstyle ee}}oldsymbol{x}_k$$





State transition function:

$$\boldsymbol{x}_k = \boldsymbol{A} \boldsymbol{x}_{k-1} + \boldsymbol{v}_k$$

Observation functions:

$$oldsymbol{y}_{ extsf{A},k} = oldsymbol{\mathcal{C}}_{ extsf{A}}oldsymbol{x}_k + oldsymbol{w}_{ extsf{A},k}$$

$$oldsymbol{y}_{{\scriptscriptstyle extsf{v}},k}=oldsymbol{\mathcal{C}}_{{\scriptscriptstyle extsf{v}}}oldsymbol{x}_k+oldsymbol{w}_{{\scriptscriptstyle extsf{v}},k}$$

 $\hat{\Sigma}_{k-1}$   $\hat{x}_{k-1}$ 

 $\hat{\pmb{x}}_{k-1}$  $\hat{\pmb{\Sigma}}_{k-1}$ 







## Dynamic stream weights



#### Inference

Prediction step (identical to standard Kalman filter)

$$egin{aligned} \hat{x}_{k|k-1} &= oldsymbol{A} \hat{x}_{k-1} \ \hat{oldsymbol{\Sigma}}_{k|k-1} &= oldsymbol{A} \hat{oldsymbol{\Sigma}}_{k-1} oldsymbol{A}^{ ext{T}} + oldsymbol{Q} \end{aligned}$$

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 $\hat{\mathbf{\Sigma}}_{k|k-1} = \mathbf{A}\hat{\mathbf{\Sigma}}_{k-1}\mathbf{A}^{\mathrm{T}} + \mathbf{Q}$ 

#### Update step<sup>1</sup>

$$\begin{bmatrix} \boldsymbol{K}_{A,k}^{\mathrm{T}} \\ \boldsymbol{K}_{V,k}^{\mathrm{T}} \end{bmatrix} = \begin{bmatrix} \boldsymbol{R}_{A} + \lambda_{A,k} \boldsymbol{C}_{A,k} \hat{\boldsymbol{\Sigma}}_{k|k-1} \boldsymbol{C}_{A,k}^{\mathrm{T}} & \lambda_{V,k} \boldsymbol{C}_{A,k} \hat{\boldsymbol{\Sigma}}_{k|k-1} \boldsymbol{C}_{V,k}^{\mathrm{T}} \\ \lambda_{A,k} \boldsymbol{C}_{V,k} \hat{\boldsymbol{\Sigma}}_{k|k-1} \boldsymbol{C}_{A,k}^{\mathrm{T}} & \boldsymbol{R}_{V} + \lambda_{V,k} \boldsymbol{C}_{V,k} \hat{\boldsymbol{\Sigma}}_{k|k-1} \boldsymbol{C}_{V,k}^{\mathrm{T}} \end{bmatrix}^{-1} \begin{bmatrix} \boldsymbol{C}_{A,k} \\ \boldsymbol{C}_{V,k} \end{bmatrix} \hat{\boldsymbol{\Sigma}}_{k|k-1} \\ \hat{\boldsymbol{x}}_{k} = \hat{\boldsymbol{x}}_{k|k-1} + \sum_{i \in \{A, V\}} \lambda_{i,k} \boldsymbol{K}_{i,k} (\boldsymbol{y}_{i,k} - \boldsymbol{C}_{i} \hat{\boldsymbol{x}}_{k|k-1}) \\ \hat{\boldsymbol{\Sigma}}_{k} = \left( \boldsymbol{I} - \sum_{i \in \{A, V\}} \lambda_{i,k} \boldsymbol{K}_{i,k} \boldsymbol{C}_{i} \right) \hat{\boldsymbol{\Sigma}}_{k|k-1} \end{aligned}$$

<sup>1</sup>Christopher Schymura and Dorothea Kolossa. "Audiovisual Speaker Tracking using Nonlinear Dynamical Systems with Dynamic Stream Weights". In: IEEE/ACM Transactions on Audio, Speech, and Language Processing, 2020

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<sup>&</sup>lt;sup>2</sup>Tuomas Haarnoja, Anurag Ajay, Sergey Levine and Pieter Abbeel. "Backprop KF: Learning Discriminative Deterministic State Estimators". In: Advances in Neural Information Processing Systems, 2016

## Proposed system

End-to-end optimization in a deep learning framework:



## Proposed system

► Learning noise covariance matrices via Cholesky decomposition:

$$\boldsymbol{q} = \begin{bmatrix} q_1 \\ q_2 \\ \vdots \\ q_N \end{bmatrix} \Rightarrow \boldsymbol{L}_{\boldsymbol{Q}} = \begin{bmatrix} q_1 & 0 & \cdots & 0 \\ q_2 & q_3 & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ q_{N-3} & q_{N-2} & q_{N-1} & q_N \end{bmatrix} \Rightarrow \boldsymbol{Q} = \boldsymbol{L}_{\boldsymbol{Q}} \boldsymbol{L}_{\boldsymbol{Q}}^{\mathrm{T}}$$

with  $\boldsymbol{Q} \in \mathbb{R}^{D imes D}$  and  $N = \frac{D(D+1)}{2}$ .

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Projecting state space to direction-of-arrival in the loss function:

$$\mathcal{L} = rac{1}{BK}\sum_{b=1}^{B}\sum_{k=1}^{K} \|oldsymbol{\mathcal{C}}_{artheta} \hat{oldsymbol{x}}_k^{(b)} - artheta_k^{(b)}\|_2^2$$

### Evaluation

Dataset: 70 audiovisual recordings of 7 speakers in an office environment, augmented with different acoustic noise conditions at 4 SNRs. 7-fold cross validation paradigm with 50/10/10 sequences train/val/test split.

#### ► Training parameters:

Parameter	Description	Value
$D_{z_A}$	Audio feature dimension (SRP-PHAT spectrum)	481
$D_{z_V}$	Video feature dimension (facial landmarks)	136
$D_{y_{A}}$ , $D_{y_{V}}$	Audio and video observation dimensions	4
$D_x$	State dimension	8
$\eta$	Learning rate	0.001
В	Batch size	128

#### Results



**Gross accuracy:** Percentage of speakers detected correctly within a radius of 2° around the annotated ground-truth direction-of-arrival.

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## Thank you for your attention!