Learning Dynamic Stream Weights for Multimodal Dynamical System Models

68. Sitzung der ITG-Fachgruppe "Signalverarbeitung und maschinelles Lernen"

Christopher Schymura and Dorothea Kolossa

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Speaker position x_k









Prediction step

System dynamics:

$$oldsymbol{x}_k = f(oldsymbol{x}_{k-1}) + oldsymbol{v}_k, \quad oldsymbol{v}_k = \mathcal{N}(oldsymbol{0}, oldsymbol{Q})$$



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$$p(\mathbf{x}_{k} | \mathbf{Y}_{A,k-1}, \mathbf{Y}_{V,k-1}) = \int p(\mathbf{x}_{k} | \mathbf{x}_{k-1}) p(\mathbf{x}_{k-1} | \mathbf{Y}_{A,k-1}, \mathbf{Y}_{V,k-1}) d\mathbf{x}_{k-1}$$

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$$p(\mathbf{x}_{k} \mid \mathbf{Y}_{\mathsf{A},k-1}, \ \mathbf{Y}_{\mathsf{V},k-1}) = \int \underbrace{p(\mathbf{x}_{k} \mid \mathbf{x}_{k-1})}_{\mathsf{Dynamic model}} \underbrace{p(\mathbf{x}_{k-1} \mid \mathbf{Y}_{\mathsf{A},k-1}, \ \mathbf{Y}_{\mathsf{V},k-1})}_{\mathsf{Prior}} d\mathbf{x}_{k-1}$$

Observation

Observation model:

$$\mathbf{y}_{k} = \begin{bmatrix} \mathbf{y}_{\mathrm{A},k} & \mathbf{y}_{\mathrm{V},k} \end{bmatrix}^{\mathsf{T}} = h(\mathbf{x}_{k}) + \mathbf{w}_{k}$$
$$\mathbf{w}_{k} = \mathcal{N}(\mathbf{0}, \mathbf{R}), \quad \mathbf{R} = \begin{bmatrix} \mathbf{R}_{\mathrm{AA}} & \mathbf{R}_{\mathrm{AV}} \\ \mathbf{R}_{\mathrm{VA}} & \mathbf{R}_{\mathrm{VV}} \end{bmatrix}$$



Update step (standard Kalman filter)

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 $p(m{x}_k \mid m{Y}_{ extsf{A},k}, \ m{Y}_{ extsf{V},k}) \propto p(m{x}_k \mid m{Y}_{ extsf{A},k-1}, \ m{Y}_{ extsf{V},k-1}) \, p(m{y}_{ extsf{A},k}, \ m{y}_{ extsf{V},k} \mid m{x}_k)$

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Update step (Kalman filter with dynamic stream weights¹)

Observation model:

$$egin{aligned} &oldsymbol{y}_{ extsf{A},k} = h_{ extsf{A}}(oldsymbol{x}_k) + oldsymbol{w}_{ extsf{A},k}, &oldsymbol{w}_{ extsf{A},k} = \mathcal{N}(oldsymbol{0}, oldsymbol{R}_{ extsf{A} extsf{A}}) \ &oldsymbol{y}_{ extsf{V},k} = h_{ extsf{V}}(oldsymbol{x}_k) + oldsymbol{w}_{ extsf{V},k}, &oldsymbol{w}_{ extsf{V},k} = \mathcal{N}(oldsymbol{0}, oldsymbol{R}_{ extsf{V} extsf{V}}) \end{aligned}$$



¹C. Schymura et al.: Extending linear dynamical systems with dynamic stream weights for audiovisual speaker localization, IWAENC, 2018

Update step (Kalman filter with dynamic stream weights¹)



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Extended Kalman filter approach: first-order Taylor series expansion

$$f(\boldsymbol{x}_{k-1}) \approx f(\hat{\boldsymbol{x}}_{k-1}) + \boldsymbol{F}(\hat{\boldsymbol{x}}_{k-1})(\boldsymbol{x}_{k-1} - \hat{\boldsymbol{x}}_{k-1})$$

Extended Kalman filter approach: first-order Taylor series expansion

$$\begin{split} f(\mathbf{x}_{k-1}) &\approx f(\hat{\mathbf{x}}_{k-1}) + \mathbf{F}(\hat{\mathbf{x}}_{k-1})(\mathbf{x}_{k-1} - \hat{\mathbf{x}}_{k-1}) \\ \Rightarrow \qquad p(\mathbf{x}_k \mid \mathbf{x}_{k-1}) &= \mathcal{N}\Big(\mathbf{x}_k \mid f(\hat{\mathbf{x}}_{k-1}) + \mathbf{F}(\hat{\mathbf{x}}_{k-1})(\mathbf{x}_{k-1} - \hat{\mathbf{x}}_{k-1}), \ \mathbf{Q}\Big) \\ \Rightarrow \qquad p(\mathbf{x}_k \mid \mathbf{Y}_{\mathsf{A},k-1}, \ \mathbf{Y}_{\mathsf{V},k-1}) &= \mathcal{N}\Big(\mathbf{x}_k \mid \hat{\mathbf{x}}_{k-1}, \ \hat{\mathbf{\Sigma}}_{k-1}\Big) \end{split}$$

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Prediction step (identical to standard EKF)

$$\begin{split} \hat{\mathbf{x}}_{k|k-1} &= f(\hat{\mathbf{x}}_{k-1}) \\ \hat{\mathbf{\Sigma}}_{k|k-1} &= \mathbf{F}_{k-1} \hat{\mathbf{\Sigma}}_{k-1} \mathbf{F}_{k-1}^{\mathsf{T}} + \mathbf{Q}, \qquad \mathbf{F}_{k-1} \equiv \mathbf{F}(\hat{\mathbf{x}}_{k-1}) = \frac{\partial f(\mathbf{x}_{k-1})}{\partial \mathbf{x}_{k-1}} \Big|_{\mathbf{x}_{k-1} = \hat{\mathbf{x}}_{k-1}} \end{split}$$

Extended Kalman filter approach: first-order Taylor series expansion

$$h_{\{\mathsf{A},\mathsf{V}\}}(oldsymbol{x}_k) pprox h_{\{\mathsf{A},\mathsf{V}\}}(\hat{oldsymbol{x}}_k) + oldsymbol{H}_{\{\mathsf{A},\mathsf{V}\},k}(oldsymbol{x}_k - \hat{oldsymbol{x}}_k), \quad oldsymbol{H}_{\{\mathsf{A},\mathsf{V}\},k} \equiv rac{\partial h_{\{\mathsf{A},\mathsf{V}\}}\left(oldsymbol{x}_k
ight)}{\partialoldsymbol{x}_k}\Big|_{oldsymbol{x}_k = \hat{oldsymbol{x}}_k}$$

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$$\begin{split} h_{\{\mathsf{A},\mathsf{V}\}}(\mathbf{x}_k) &\approx h_{\{\mathsf{A},\mathsf{V}\}}(\hat{\mathbf{x}}_k) + \mathbf{H}_{\{\mathsf{A},\mathsf{V}\},k}(\mathbf{x}_k - \hat{\mathbf{x}}_k), \quad \mathbf{H}_{\{\mathsf{A},\mathsf{V}\},k} \equiv \frac{\partial h_{\{\mathsf{A},\mathsf{V}\}}(\mathbf{x}_k)}{\partial \mathbf{x}_k} \Big|_{\mathbf{x}_k = \hat{\mathbf{x}}_k} \\ &\Rightarrow \qquad p(\mathbf{y}_{\{\mathsf{A},\mathsf{V}\},k} \mid \mathbf{x}_k) = \mathcal{N}\Big(\mathbf{y}_{\{\mathsf{A},\mathsf{V}\},k}, \mid h_{\{\mathsf{A},\mathsf{V}\}}(\hat{\mathbf{x}}_k) + \mathbf{H}_{\{\mathsf{A},\mathsf{V}\},k})(\mathbf{x}_k - \hat{\mathbf{x}}_k), \ \mathbf{R}_{\{\mathsf{A},\mathsf{V}\}}\Big) \end{split}$$

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Update step

$$\begin{bmatrix} \mathbf{K}_{\mathsf{A},k}^{\mathsf{T}} \\ \mathbf{K}_{\mathsf{V},k}^{\mathsf{T}} \end{bmatrix} = \begin{bmatrix} \mathbf{R}_{\mathsf{A}} + \lambda_{k} \mathbf{H}_{\mathsf{A},k} \hat{\mathbf{\Sigma}}_{k|k-1} \mathbf{H}_{\mathsf{A},k}^{\mathsf{T}} & (1-\lambda_{k}) \mathbf{H}_{\mathsf{A},k} \hat{\mathbf{\Sigma}}_{k|k-1} \mathbf{H}_{\mathsf{V},k}^{\mathsf{T}} \\ \lambda_{k} \mathbf{H}_{\mathsf{V},k} \hat{\mathbf{\Sigma}}_{k|k-1} \mathbf{H}_{\mathsf{A},k}^{\mathsf{T}} & \mathbf{R}_{\mathsf{V}} + (1-\lambda_{k}) \mathbf{H}_{\mathsf{V},k} \hat{\mathbf{\Sigma}}_{k|k-1} \mathbf{H}_{\mathsf{V},k}^{\mathsf{T}} \end{bmatrix}^{-1} \begin{bmatrix} \mathbf{H}_{\mathsf{A},k} \\ \mathbf{H}_{\mathsf{V},k} \end{bmatrix} \hat{\mathbf{\Sigma}}_{k|k-1} \\ \hat{\mathbf{x}}_{k} = \hat{\mathbf{x}}_{k|k-1} + \lambda_{k} \mathbf{K}_{\mathsf{A},k} \Big(\mathbf{y}_{\mathsf{A},k} - \mathbf{h}_{\mathsf{A}} (\hat{\mathbf{x}}_{k}) \Big) + (1-\lambda_{k}) \mathbf{K}_{\mathsf{V},k} \Big(\mathbf{y}_{\mathsf{V},k} - \mathbf{h}_{\mathsf{V}} (\hat{\mathbf{x}}_{k}) \Big) \\ \hat{\mathbf{\Sigma}}_{k|k-1} = \Big(\mathbf{I} - \lambda_{k} \mathbf{K}_{\mathsf{A},k} \mathbf{H}_{\mathsf{A},k} - (1-\lambda_{k}) \mathbf{K}_{\mathsf{V},k} \mathbf{H}_{\mathsf{V},k} \Big) \hat{\mathbf{\Sigma}}_{k|k-1}$$

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Evaluation I

Experimental setup

▶ KAVTraC audiovisual dataset, recorded in an office room at RUB using the Kinect sensor (7 speakers, $T_{60} \approx 350 \,\mathrm{ms}$, 35 min. duration).



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- Constant velocity linear dynamics model and nonlinear rotating vector observation models.
- ► DSW-EKF uses Dirichlet-prior oracle DSWs².



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- DSW-EKF uses Dirichlet-prior oracle DSWs².
- Four baseline systems: standard EKF, one KF-based and two particle filter-based systems.
- Leave-one-out cross-validation paradigm.



Evaluation I

Results



³T. Gehrig et al.: Kalman filters for audio-video source localization, WASPAA, 2005
 ⁴S. Gerlach et al.: 2D audio-visual localization in home environments using a particle filter, ITG Symp., 2012
 ⁵X. Qian et al.: 3D audio-visual speaker tracking with an adaptive particle filter, ICASSP, 2017

Standard approach: Supervised training with oracle dynamic stream weights



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Proposed approach: Training with natural evolution strategies



Training procedure⁶



Training procedure⁶



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Training procedure⁶



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Training procedure⁶



Evaluation II

Results



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